

# Crystallization kinetics of GdYScAlCo high-entropy bulk metallic glass

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## Abstract

The thermal stability and non-isothermal crystallization of a new bulk-amorphous high-entropy (HE-BMG) equiatomic GdYScAlCo alloy were studied by differential scanning calorimetry (DSC). The alloy shows a four-stage crystallization process. The kinetic parameters (activation energy ( $E_a$ )), the pre-exponential factor ( $\log A$ ) and glass-forming ability indicators (kinetic fragility index, characteristic temperatures) for the GdYScAlCo alloy were obtained. The  $E_a$  values obtained by isoconversional methods indicate a nonlinear Arrhenian behaviour and a complex process. The Avrami equation modification proposed by Jeziorny and the multivariate nonlinear regression method were applied on the nonisothermal crystallization. In the case of primary crystallization of the amorphous GdYScAlCo alloy under nonisothermal conditions, the kinetics of the nucleation process is best described by an autocatalytic reaction.

## Keywords

high-entropy bulk metallic glass  
activation energy  
glass-forming ability  
primary crystallization

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## Key findings

- New bulk-amorphous high-entropy equiatomic GdYScAlCo alloy was produced.
- Non-isothermal crystallization kinetics of GdYScAlCo metallic glass was investigated.
- The multivariate nonlinear regression method suggested a combined auto-catalysis reaction model.

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## 1. Introduction

Since the first discovery in 1960, interest in metal glasses and other metastable materials has been growing [1]. For more than 60 years of research, several hundred bulk metallic glasses (BMG) were synthesized with dimensions up to tens of centimeters. The majority of the synthesized BMGs are alloys based on one or two basic elements with small additions of elements that increase glass-forming ability and characteristics of materials [2–4]. In addition to high glass-forming ability, such materials have a number of unique properties: high thermal stability, high plasticity and soft magnetic properties.

Also, amorphous alloys based on Sc–Al–Co have unique strength and corrosion characteristics [5]. Additionally, additives of rare-earth metals (REM) affect the glass-forming

ability (GFA) of these alloys. For example, REM additives (Gd, Y) increase the glass-forming ability and improve the mechanical properties of Sc–Al–Co alloys [5].

However, the GFA and thermal stability of GdYScAlCo alloys, as well as the mechanisms of their crystallization, is not studied. We chose an equiatomic GdYScAlCo alloy for research because it easily amorphizes under arc melting conditions. To estimate the GFA, we used various experimental indicators of glasses, such as glass transition temperature ( $T_g$ ), on-set crystalline temperature ( $T_x$ ) and liquidus temperature ( $T_l$ ), etc.

To obtain given properties of the GdYScAlCo alloy, as well as to predict the optimal compositions and heat treatment modes, the calculation of kinetic parameters (activation energy  $E_a$ , pre-exponential factor) using iso-conversion methods of thermal analysis was carried out.

## 2. Experimental procedure

### 2.1. Materials and synthesis

The master equiatomic GdYScAlCo alloy was prepared by arc melting Al (99.99% purity), Gd (99.9%), Y (99.9%), Sc (99.9%) and Co (99.9%) in a helium atmosphere. Further, it is re-melted five times to achieve complete melting and compositional homogeneity. The composition of the samples was controlled by weighing them before and after synthesis, and the mass loss did not exceed 0.1 wt.%. Then, amorphous alloy was produced by performing suction casting of the arc-melted metal liquid into a copper mold to produce a 3 mm diameter rod.

### 2.2. Differential scanning calorimetry (DSC) and X-ray diffraction measurements

The as-cast rod structure was examined by X-ray diffraction at room temperature in a  $2\theta$  angular range of  $25^\circ$ – $100^\circ$  at a step of  $0.004^\circ$  using a Shimadzu XRD7000 diffractometer and Cu  $K\alpha$  radiation; the exposition time was 3 s. Thermal reactions in the sample were investigated by differential scanning calorimetry using a Netzsch STA 449C device, calibrated with indium, tin zinc, aluminum, silver and gold standards. The selected sample mass was  $20.1 \pm 0.1 \cdot 10^{-6}$  kg. DSC scans were performed at different heating rates (5, 10, 20, 40 K/min) in the temperature range from 273 to 1100 K at an argon flow of 60 ml/min. To describe the initial crystallization process and to determine the kinetic parameters, NETZSCH Kinetics Neo software (NETZSCH, Selb, Germany) was applied using model-free and the multivariate nonlinear regression methods.

## 3. Results and Discussion

### 3.1. Thermal analysis and GFA indicators

Figure 1 illustrates an X-ray pattern of the GdYScAlCo rod that shows an amorphous halo without distinct crystalline peaks, i.e., the resulting sample is X-ray amorphous.

The non-isothermal DSC of GdYScAlCo HE-BMG are shown in Figure 2. All the DSC curves exhibit the four exothermic reactions corresponding to the crystallization processes. Table 1 shows the thermal characteristics of the GdYScAlCo alloy: glass transition temperature  $T_g$ , on-set crystalline temperature  $T_x$ , melting temperature  $T_m$ , liquidus temperature  $T_l$ , as well as indicators of glass-forming ability: supercooled liquid interval  $\Delta T_x = T_g - T_x$ ,  $T_{rg} = T_l/T_g$  and melting interval  $\Delta T_l = T_l - T_m$ . GdYScAlCo alloy shows high values of glass transition temperature  $T_g$ .

GFA is related to physical nature of alloy and reflects how well the alloy forms metallic glass during casting. There are various criteria for evaluating GFA, including  $\gamma$  and  $\delta$ , which are based on the classical theory of nucleation [6]. These criteria can be easily obtained by thermal analysis and show a strong correlation with GFA in metallic

glasses. Calculation of  $\gamma$  and  $\delta$  criteria was carried out according to equations:

$$\delta = \frac{T_x}{(T_l - T_g)} \quad (1)$$

$$\gamma = \frac{T_x}{(T_l + T_g)} \quad (2)$$

In paper [7] for the four-component  $\text{Sc}_{36}\text{Al}_{24}\text{Co}_{20}\text{Y}_{20}$  alloy the value of the criterion  $\gamma = 0.444$  was presented, which agrees well with our data for the five-component GdYScAlCo alloy ( $\gamma = 0.407$ ). Table 1 shows the criteria  $\gamma$  and  $\delta$ , which indicate a good glass forming ability of the GdYScAlCo alloy.

The term “fragility” introduced by Angel [8], shows the degree of deviation of the temperature dependence of the viscosity from the Arrhenius curve and is a GFA indicator. From the physical perspective, it characterizes how well the material transitions to the glass state when cooled. Substances with high values of this parameter have a narrow range of glass transition temperatures, while substances with low values have a relatively wide range [8].

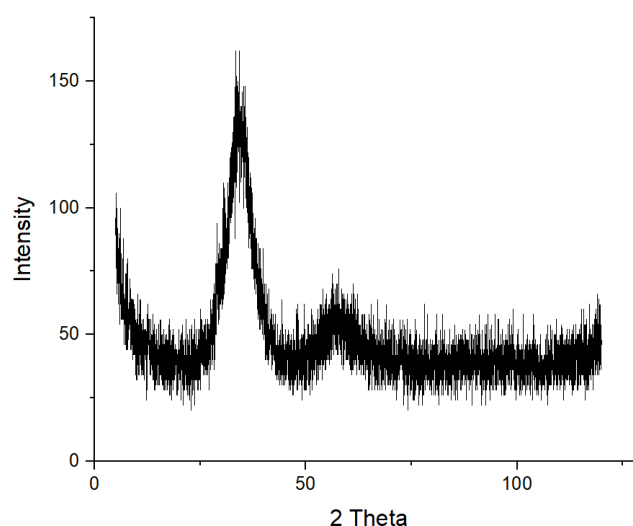


Figure 1 XRD pattern of the GdYScAlCo rod.

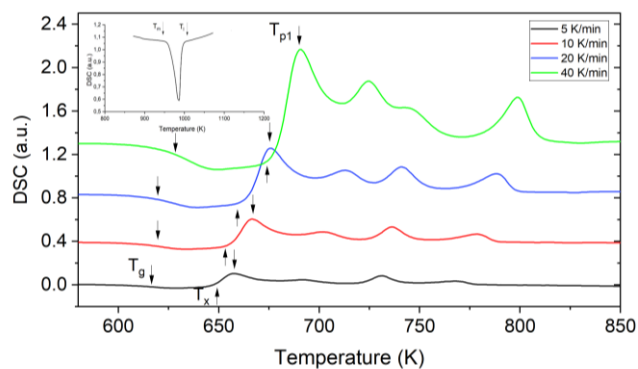


Figure 2 Experimental DSC curves of GdYScAlCo amorphous alloy at different heating rates (inset: temperatures  $T_m$ ,  $T_l$  for heating rate of 10 K/min).

**Table 1** Thermal characteristics for GdYScAlCo alloy according to DSC measurements obtained at a rate of 10 K/min.

Alloy	$T_g$ , K	$T_x$ , K	$T_m$ , K	$T_l$ , K	$\Delta T_x$	$T_{rg}$	$\Delta T_l$	$\gamma$	$\delta$
GdYScAlCo	559	631.5	960	992	32	0.563	32	0.407	1.458

Fragility is determined by the slope of the viscosity curve according to the dependence of  $\log(\text{viscosity})$  on  $T_g/T$  when approaching  $T_g$ , which gives the kinetic index of a Fragility ( $m$ ). The kinetic a Fragility index can be obtained as follows [9]:

$$m = \frac{DT_0T_g}{(T_g - T_0)^2 \ln 10} \quad (3)$$

where  $D$  is the strength parameter,  $T_0$  is the asymptotic value of  $T_g$  at an infinitely slow cooling and heating rate, and  $T_g$  is the glass transition temperature [8].  $D$  and  $T_0$  can be determined through the relationship between  $T_g$  and heating rate ( $\beta$ ) by an equation with the Vogel-Fulcher-Tammann form [10]:

$$\ln \beta = \ln(B) - \frac{DT_0}{T_g - T_0} \quad (4)$$

Fragility index for the sample was calculated at heating rates 5, 10, 20, 40 K/min. The data obtained from Equations 3 and 4 are summarized in Figure 3. The results show that  $m$  is equal to 33. The liquids with the fragility index  $m$  close to 17 are usually referred to “strong” glass-formers. The liquids with  $m$  much higher than 17 are usually referred to “fragile”. In the case of GdYScAlCo HE-BMG, it can be classified into “fragile” glasses.

The parameter  $F_1$ , introduced by Senkov [11], is an indicator of glass-forming ability, which establishes a correlation between the fragility parameter and the critical cooling rate at which the amorphous state is formed. The value  $F_1 = 0$  corresponds to an extremely fragile liquid, and  $F_1 \sim 0.8$  – extremely strong liquid.

The  $F_1$  parameter can be defined as:

$$F_1 = \frac{(T_g - T_0)}{0.5(T_l + T_g) - T_0} \quad (5)$$

where  $T_g$  is the glass transition temperature,  $T_l$  is the liquidus temperature, and  $T_0$  is the on-set temperature.

The calculation results are presented in Table 2.

Compared to other metallic glasses: La<sub>55</sub>Al<sub>25</sub>Ni<sub>20</sub> ( $m = 42$ ,  $F_1 = 0.455$ ), La<sub>55</sub>Al<sub>25</sub>Ni<sub>10</sub>Cu<sub>10</sub> ( $m = 35$ ,  $F_1 = 0.540$ ) [11], the alloy GdYScAlCo shows rather high values in fragility and the  $F_1$  parameter, which indicates its good glass forming ability.

## 3.2. Primary crystallization kinetics of GdYScAlCo

### 3.2.1. Activation energy

One of the most important kinetic parameters of the crystallization process is the activation energy. It represents the energy barrier that must be overcome by the system to start the nucleation and growth process leading to crystallization.

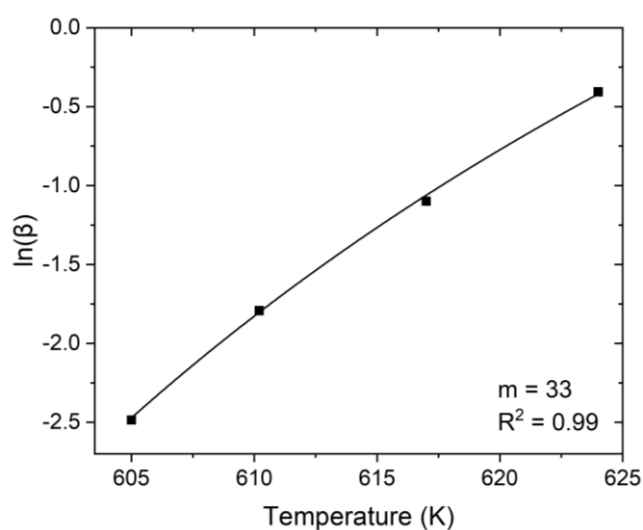
According to Figure 2, there are four crystallization peaks on the DSC curves. Since the first peak overlaps with

the second and third ones, we used a mathematical procedure of peak shape separation to correctly estimate the kinetic parameters of the nucleation and primary crystallization process (Figure 4) [12]. In the calculations we used the DSC peaks at different heating rates obtained by deconvolution, so they should be compared. The separated peaks have the same shape at different heating speeds, i.e., they are identical to each other. As can be seen in Figure 4, the positions of onset and peak maximum temperatures of the original DSC signal and the separated ones are almost the same. The baseline was a straight line. Because the crystallization of amorphous alloy is a multistage process, it requires additional structural studies. Here, we limit ourselves to calculating the kinetic parameters only for the first peak and describing the mechanism of nucleation and primary crystallization. Thus, the DSC curves (Figure 2) show peaks corresponding to the nucleation and crystal growth processes. We calculate the activation energies corresponding to these temperatures to understand the nucleation and crystallization in general.

In the methods of non-isothermal kinetics based on the free model, it is assumed that the single-step processes occurring can be described following rate equation [13]:

$$\beta \frac{da}{dt} = Af(a)e^{-\frac{E_a}{RT}}, \quad (6)$$

where  $A$  is the pre-exponential factor,  $\beta$  – the constant heating rate,  $E_a$  is the activation energy, and the concentration dependence of the reaction rate (reaction model) is  $f(a)$ , where  $a$  is the degree of transformation of the substance in the range from 0 to 1.

**Figure 3** Fragility index for GdYScAlCo alloy.**Table 2**  $T_g$ ,  $T_l$ ,  $m$  and  $F_1$  parameter for GdYScAlCo alloy.

$T_g$ (K)	$T_l$ (K)	$m$	$F_1$
559	992	33	0.463

Additionally, it was assumed that the reaction rate at a constant conversion value depends only on temperature (iso-conversion principle). It should be noted the importance of determining the preexponential factor  $A$  in the framework of kinetic analysis without using a model. According to Vyazovkin [14] model-free method of estimating the preexponential factor  $A$  is suitable for both single- and multi-step kinetics. Model-free methods of analysis allow us to determine the activation energy  $E_a$  of the reaction process without making hypotheses about the kinetic model of the process and without knowing the type of reaction [13]. Various model-free methods are used to calculate the activation energy  $E_a$  of non-isothermal reactions at different heating rates [15–17]. First, we used the most common of them, the Kissinger method. The basic equation of the Kissinger method is written as

$$\ln(\beta/T^2) = -E/RT + \text{const}, \quad (7)$$

where  $\beta$  is the heating rate,  $R$  is the gas constant,  $T$  is the temperature.

Figure 5 shows the dependences described by equation (2), which correspond to the following processes: the glass transition at  $T_g(E_g)$ ; the start of nucleation at  $T_x(E_x)$ ; the crystal growth at  $T_{p1}(E_{p1})$ . The calculation results of the activation energy are shown in Figure 5 and Table 3.

Table 4 shows that the highest activation energy is at the beginning of the nucleation process,  $E_x = 314$  kJ/mol. This suggests that the most energy-consuming process is the beginning of crystallization (the appearance of the first nuclei of the crystalline phase in the amorphous matrix).

Thus, we determined the activation energy of the primary crystallization process ( $E_p$ ) using the Kissinger equation (Equation 7). However, from a physical viewpoint, this method cannot be applied directly to amorphous alloys, since the crystallization process in them proceeds through the nucleation and crystal growth processes rather than through the n-order reaction [18, 19]. Also, as noted by Vyazovkin [13], Kissinger's method is not very accurate. The method gives a single activation energy in accordance with the assumption of one-step kinetics, which creates a problem for most applications.

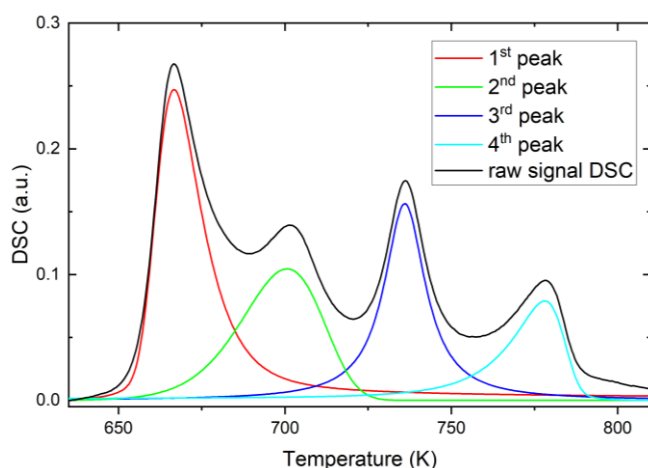


Figure 4 Separated DSC curves for a heating rate of 10 K/min.

We performed calculations of  $E_a$  using other model-free methods (Vyazovkin [15], Friedman [16] and Ozawa [17]) in the NETZCH Kinetics Neo software. The calculation results by Kissinger, Vyazovkin, Friedman and Ozawa methods are presented in Table 4 and Figure 5. The analysis of the dependence of  $E_a$  versus  $\alpha$  (conversion) of the crystallization process of the HE-BMG GdYScAlCo alloy obtained from iso-conversional methods (Ozawa, Friedman and Vyazovkin) allows us to check the applicability of the one-step kinetics according to Equation 7.

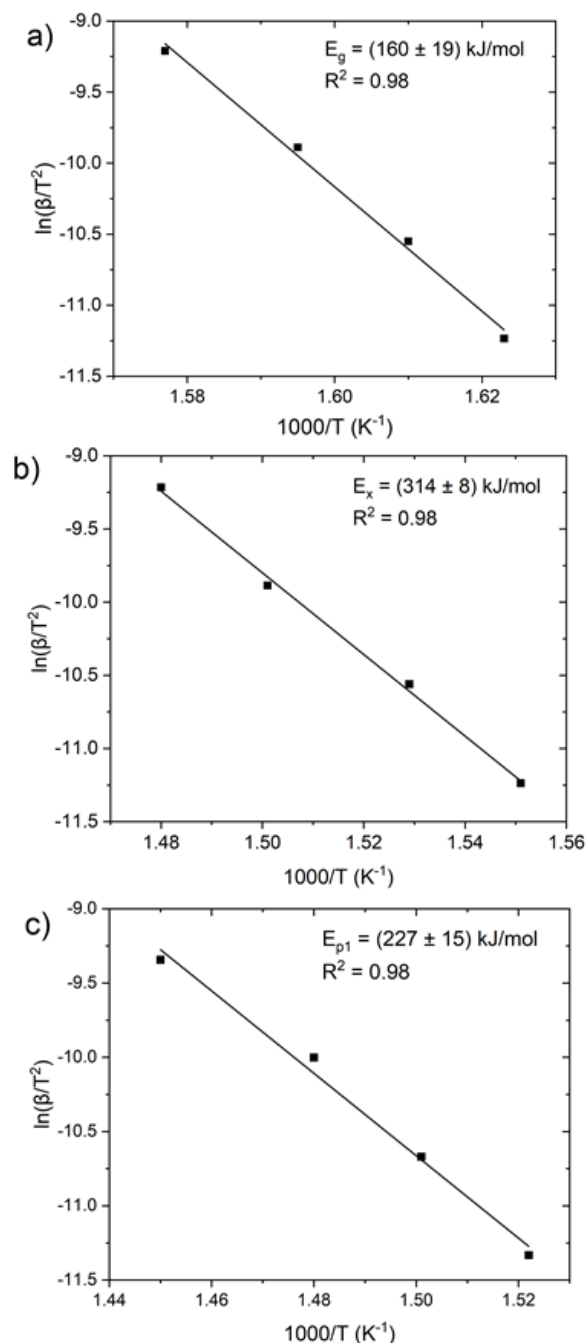


Figure 5 Kissinger plots for calculating activation energies in GdYScAlCo BMG.

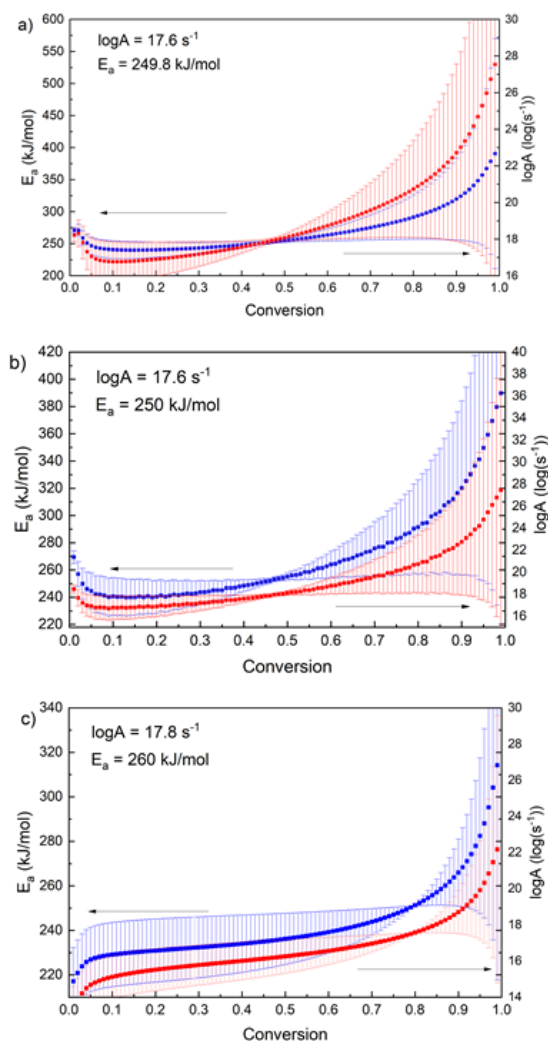
Table 3 Activation energy  $E_g$ ,  $E_x$ ,  $E_{p1}$  for temperatures  $T_g$ ,  $T_x$ ,  $T_{p1}$ .

Alloy	Activation energy, kJ/mol		
	$E_g$	$E_x$	$E_{p1}$
GdYScAlCo	160	314	227

Figure 4 presents the dependence of the  $E_\alpha$  and  $\log A$  on the degree of conversion calculated using Ozawa, Friedman and Vyazovkin methods. We can see from Figure 6 that the values of  $E(\alpha)$  change nonlinearly, whereas the dependences of  $E(\alpha)$  are similar. The  $E_\alpha$  values indicate a nonlinear Arrhenian behaviour and a complex process. The close average  $E(\alpha)$  values obtained by the conversional methods differ from those calculated with Kissinger's method. Therefore, the Kissinger method can only be used for preliminary estimation of the activation energy of a one-step process. Due to the fact that the values of  $E(\alpha)$  change nonlinearly and indicate a complex process, naturally, the Kissinger activation energy values cannot be applied when simulating the complex process of crystallization of amorphous materials, where multistage processes are observed.

**Table 4** Crystal growth activation energy  $E_{p1}$  and pre-exponential factor  $\log A$  for GdYScAlCo alloy.

Kinetic parameter	Vyazovkin	Kissinger method	Friedman	Ozawa-Flynn-Wall	Average value
$E_{p1}$ ,	250	227	250	260	247
$\log A$	17.6	13.1	17.6	17.8	16.5



**Figure 6** Activation energy and  $\log A$  values of versus conversion during the crystallization process using the Friedman (a), Vyazovkin (b), and Ozawa (c) methods.

### 3.2.2. Avrami model using Jeziorny method

One of the most commonly used models for describing the crystallization kinetics of polymers, metals, and glasses is the Avrami model (also known as the Johnson-Mehl-Avrami-Erofeev-Kolmogorov (JMAEK) model [20-25]). To isothermal conditions, the Avrami equation is typically used in the following form:

$$a(T) = 1 - e^{-k(T) \cdot t^n}, \quad (8)$$

where  $a$  is the degree of conversion,  $k(T)$  represents the rate constant,  $t$  is time and  $n$  is the local Avrami index.

For nonisothermal experimental conditions, Equation (8) is frequently expressed as the following linear equation:

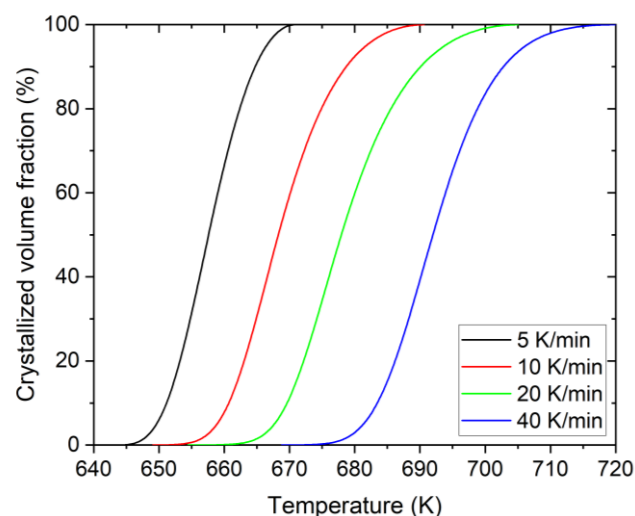
$$\frac{da}{dt} = \frac{k(T)}{\beta} \cdot n \cdot (1-a) \cdot [-\ln(1-a)] \cdot \frac{(n-1)}{n}. \quad (9)$$

The volume fraction of crystals (conversion  $a$ ) can be determined by the crystallization heat using the following equation [26]:

$$a = \frac{\int_{T_0}^T (dH/dT)dT}{\int_{T_0}^{T_{inf}} (dH/dT)dT} = \frac{A_0}{A_{inf}}, \quad (10)$$

where  $T_0$  and  $T_{inf}$  are the temperatures of the beginning and end of crystallization, respectively.  $dH$  corresponds to the enthalpy of crystallization released during an infinitesimal temperature interval  $dT$ .  $A_0$  and  $A_{inf}$  correspond to the region between the initial and specific temperature and the end of crystallization, respectively. Figure 7 shows the relationship between the volume fraction of crystallization and the temperature for primary crystallization. From Figure 7 we see that with an increase in the heating rate, the S-curves shift to the region of higher temperatures.

Many attempts have been made to derive Equation 8 under non-isothermal temperature with constant heating or cooling rates [27]. The main difficulty in modifying the JMAEK model under non-isothermal conditions is that these experiments are much faster than isothermal experiments.



**Figure 7** Crystallized volume fraction versus K temperature plots.

In isothermal experiments, the material under study is heated to a certain temperature in a time much shorter than the transformation time. Crystallization of metallic glasses under linear heating conditions is mainly studied using the JMAEK method modified by Jeziorny [28], who converted the linear Avrami equation to linear heating conditions using the following assumption:

$$\ln k_A = \frac{\ln k(T)}{\beta}, \tag{11}$$

where  $k(T) = Ae^{-\frac{E_a}{RT}}$  - rate constant,  $\beta$  - heating rate

However, as Vyazovkin states [29], this transformation contradicts the basic principle of equating physical quantities and also leads to incorrect Avrami indices, usually larger than the actual value. It should be noted that the Jeziorny's method is often used to calculate the Avrami index of non-isothermal crystallization kinetics of amorphous metallic glasses due to the developed algorithm for the interpretation of the polymer crystallization mechanism. [30]. However, the crystallization processes in amorphous metallic materials and polymers can be radically different. Further, the mechanism of primary crystallization for the amorphous GdYScAlCo alloy under non-isothermal conditions by the Jeziorny method will be tested in the multivariate nonlinear regression method. To determine the mechanism of nucleation and its growth, we used the approach of determining the local Avrami index  $n(\alpha)$  with Jeziorny's assumption (Equation 11), which was proposed in [31]. According to [31], the local Avrami index  $n(\alpha)$  can be found from a modification of the JMAEK equation, given that  $t-t_0 = (T-T_0)/\beta$ , where  $T_0$  is the temperature at the crystallization onset. Therefore, it can be written as:

$$\frac{d\ln[-\ln(1-\alpha)]}{d\{\ln[(T-T_0)/\beta]\}} = n \left\{ 1 + \frac{E}{RT} \left( 1 - \frac{T_0}{T} \right) \right\}, \tag{12}$$

where  $T_0$  is the initial crystallization temperature and  $E$  is the activation energy of the crystallization process. The values of  $E$  in Equation 10 were used as  $E(\alpha)$  calculated by the Vyazovkin method.

For non-isothermal DSC curves, the local Avrami index ( $n(\alpha)$ ) can be obtained by plotting the dependence of  $\ln[-\ln(1-\alpha)]$  on  $\ln[(T-T_0)/\beta]$ . The plots of these dependences are shown in Figure 8, where the value of  $n(\alpha)$  can be obtained from the slope of these curves. In addition, Figure 9 shows the local Avrami index indices as a function of the volume fraction of crystallized matter  $\alpha$  at different heating rates. The resulting curves are not linear, indicating that  $n(\alpha)$  changes during the crystallization process. The  $n(\alpha)$  is a basic parameter that is necessary to understand the mechanisms of nucleation and grain growth with increasing  $\alpha$  during the transformation phase. The local Avrami index is expressed as:

$$n = b + pm, \tag{11}$$

where  $b$  is the nucleation index,  $m$  is the dimensionality of grain growth and  $p$  is the type of growth. The germination

index contains four conditions: (1)  $b = 0$  suggests a zero germination rate; (2)  $0 < b < 1$  indicates a decrease in the germination rate with time; (3)  $b = 1$  represents a constant germination rate; (4)  $b > 1$  indicates an increase in the germination rate with time. The grain growth magnitude  $m$  is 1, 2, or 3;  $p = 1$  represents surface-controlled growth, and  $p = 0.5$  indicates diffusion-controlled growth.

Before describing the primary crystallisation mechanism using the  $n(\alpha)$  dependence, we present an important remark. Since the peak separation procedure performed allows determining the approximate baseline, it must be considered that extreme values of  $n(\alpha)$  (both  $\alpha <$  and  $\alpha \sim 1$ ) are unreliable, since they are affected by the baseline.

Figure 8 shows that at the start of the crystallization process, the  $n(\alpha)$  values are 2.2-3.5, indicating that the growth mechanism is surface-controlled. The appearance of these curves clearly shows the course of nucleation and grain growth at different heating rates. All  $n(\alpha)$  at different heating rates are greater than unity at  $x = 0$ , which corresponds to the nucleation process with increasing nucleation rate;  $n(\alpha)$  of the three curves (10, 20, 40 K/min) firstly increases and then decreases at  $0.05 \leq x \leq 0.91$ , which indicates that the nucleation rate and growth dimension always change at this stage. The continuous decrease of  $n(\alpha)$  values after a certain percentage of crystallization volume fraction ( $\geq 5\%$  for speeds 10-40 K/min) shows that nucleation rates decrease to about zero and the grain growth process dominates; all  $n(\alpha)$  curves increase rapidly at  $0.91 \leq x \leq 1$ .

In the initial stage of crystallization, nucleation dominates, with a constant or increasing rate and no grain growth process when  $1 \leq n(\alpha) < 2$ ; there is one ( $n(\alpha) = 2$ ), two ( $2 < n(\alpha) < 3$ ) or three-dimensional growth ( $3 \leq n(\alpha)$ ) with constant, decreasing or increasing rate of nucleation. In our case, in the initial stage of crystallization the three-dimensional growth of nuclei with increasing nucleation rate is observed.

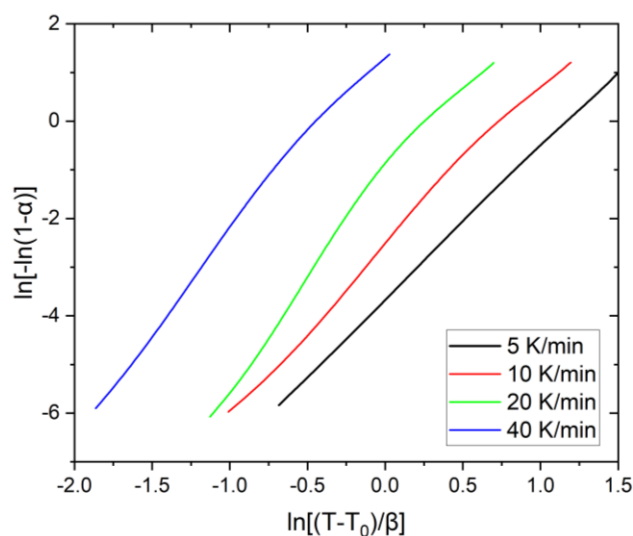


Figure 8  $\ln[-\ln(1-x)]$  versus  $\ln[(T-T_0)/\beta]$  plots at various heating rates (1<sup>st</sup> DSC peak).

At 5 K/min,  $n(\alpha)$  remains constant until  $0.5 \leq \alpha \leq 0.8$ , and then increases, indicating that the nucleation process continues at a constant rate. Thus, for the initial stage of crystallization of the amorphous GdYScAlCo alloy, there is a dependence of the nucleation process versus the heating rate.

### 3.2.3. Avrami model using the multivariate nonlinear regression method

The multivariate nonlinear regression method was also applied to the DSC data of amorphous GdYScAlCo alloy using the Avrami model. This method constructs a kinetic model of the reaction (consecutive, parallel, branched, etc.) and selects the models describing each step. Equations describing kinetic models contain several parameters which are defined by the non-linear regression method from the DSC curves approximation. A comprehensive kinetic analysis using multivariate non-linear regression was performed with NETZSCH Kinetics Neo software [32].

We verified the JMAEK method modified by Jeziorny with respect to all heating curves and the fact that the primary crystallization process is sequential and two-stage ( $A \rightarrow B \rightarrow C$ ). According to the above-described  $n(\alpha)$  relationships, the crystallization mechanism of amorphous GdYScAlCo alloy is largely determined by three-dimensional nucleation growth ( $A \rightarrow B$  ( $A_n$ )) that is surface-controlled ( $B \rightarrow C$  ( $R_3$ )). The simulation results and equations of the crystallization models are shown in Figure 10 and Table 5.

Comparative analysis shows satisfactory results (correlation coefficient  $R^2 = 0.9678$ ); the average values of the Avrami index and  $E_a$  are close to those obtained by Equation 12 and Vyazovkin (Friedman, Ozawa).

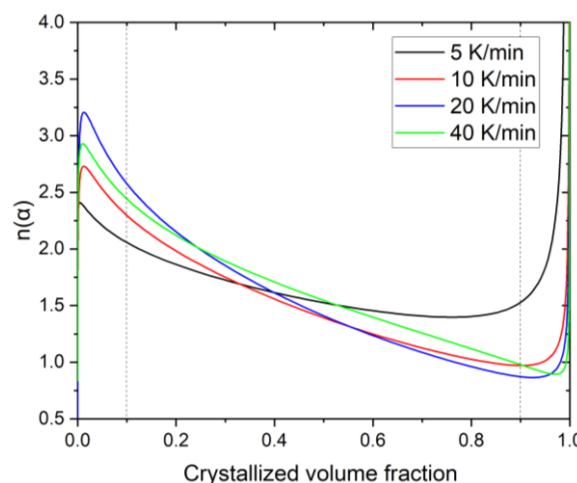
As calculated, the best correlation coefficient (0.9950) between the separated and simulated DSC curves was obtained by the combined auto-catalysis reaction as two parallel reactive paths ( $A \rightarrow B$ ,  $A+B \rightarrow 2B$ ) according to heterogeneous reaction of  $n^{\text{th}}$  order with  $m$ -Power autocatalysis by-product Kamal-Sourour [33]:

$$\frac{d\alpha}{dt} = A e^{-\frac{E_{a1}}{RT}} \cdot (1-\alpha)^n + K_{cat} \cdot A e^{-\frac{E_{a2}}{RT}} \cdot (1-\alpha)^n \cdot \alpha^m, \quad (13)$$

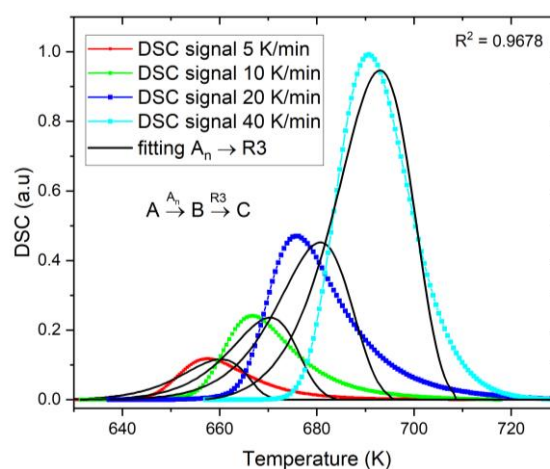
where  $k_{cat}$  - auto-catalysis factor,  $\alpha$  - conversion,  $n, m$  - reaction order,  $T$  - temperature.

The results of the simulation and equations of the crystallization model, according to the above proposed primary crystallization scheme of the amorphous GdYScAlCo alloy, are shown in Figure 11 and Table 6.

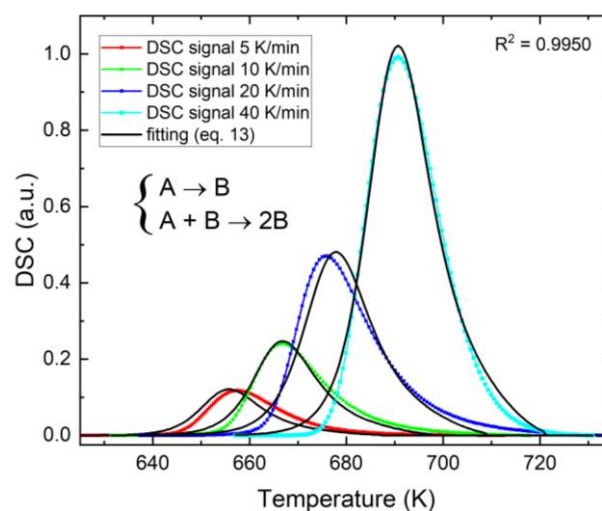
Thus, based on multivariate nonlinear regression method simulation data, the primary crystallization of the amorphous GdYScAlCo alloy proceeds as a combined auto-catalysis reaction in two parallel reactive paths.



**Figure 9** The local Avrami index  $n(\alpha)$  versus the volume fraction of crystallization ( $\alpha$ ).



**Figure 10** Crystallization model of amorphous GdYScAlCo alloy described by the three-dimensional nucleation growth ( $A \rightarrow B$  ( $A_n$ )) with surface-controlled ( $B \rightarrow C$  ( $R_3$ )).



**Figure 11** Crystallization model of amorphous GdYScAlCo alloy described by the combined auto-catalysis reaction as two parallel reactive paths ( $A \rightarrow B$ ,  $A+B \rightarrow 2B$ ).

**Table 5** Kinetic parameters and the regression coefficient  $R^2$  for the fitting of multivariate nonlinear regression according to two-stage consecutive reactions (three-dimensional nucleation growth ( $A \rightarrow B$  ( $A_n$ )) with surface-controlled ( $B \rightarrow C$  ( $R_3$ )).

$n_{A \rightarrow B}$	$\log A_{A \rightarrow B}, \log(\text{s}^{-1})$	$\log A_{B \rightarrow C}, \log(\text{s}^{-1})$	$E_{a A \rightarrow B}, \text{kJ/mol}$	$E_{a B \rightarrow C}, \text{kJ/mol}$	$C_{A \rightarrow B}$	$C_{B \rightarrow C}$	$R^2$
2.1	13.7	25.8	200.1	354.3	0.48	0.52	0.9678

**Table 6** Kinetic parameters and the regression coefficient  $R^2$  for the fitting of multivariate nonlinear regression for combined autocatalysis reaction (heterogeneous reaction with  $n$ -th order and  $m$ -power autocatalysis).

$n$	$m$	$\log A, \log(\text{s}^{-1})$	$E_a, \text{kJ/mol}$	$R^2$
1.8	0.8	12.7	216.6	0.9950

## 4. Conclusions

The thermal stability and primary crystallization kinetics of the GdYScAlCo HE-BMG alloy were studied using DSC. The main conclusions are presented below.

1. GdYScAlCo HE-BMG exhibited four different crystallization events. The characteristic temperatures (such as  $T_{x1}$ ,  $T_{p1}$ ,  $T_g$ ...) increased with increasing heating rate. In terms of  $m = 33$  and Angel's GdYScAlCo classification, HE-BMG belongs to the "fragile" glasses.

2. The activation energy ( $E_a$ ) of the process was calculated using the methods of Vyazovkin, Ozawa, Friedman and Kissinger. The Kissinger method gives inaccurate activation energy values in comparison to the other methods. The  $E_a$  values obtained by isoconversional methods indicate a nonlinear Arrhenian behaviour and a complex process.

3. Analysis of the crystallization kinetics by Jeziorny's modification of the Avrami model showed that values of the local Avrami index are  $1.2 < n(\alpha) < 3.2$  for approximately the entire initial crystallization period. This means that the crystallization mechanism is largely determined by three-dimensional nucleation growth controlled by the surface as the nucleation rate decreases. As verified by multivariate non-linear regression, the germ growth mechanism in the amorphous GdYScAlCo alloy is satisfactorily described by interface-controlled process.

4. The multivariate nonlinear regression method demonstrated that the primary crystallization of amorphous GdYScAlCo alloy proceeds as a combined auto-catalysis reaction in two parallel reactive paths ( $A \rightarrow B$ ,  $A+B \rightarrow 2B$ ), where the nucleation mechanism is determined by the heterogeneous  $n$ -th order reaction ( $A \rightarrow B$ ), and grain growth ( $A+B \rightarrow 2B$ ) by the  $m$ -power autocatalysis reaction.

## • Supplementary materials

No supplementary materials are available.

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## • Conflict of interest

The authors declare no conflict of interest.

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